

Statistics 31, Section 3, Solution to HW 4.85

4.85, ignore “Venn diagram”, as intermediate steps, find:

(a,i) $P\{\text{Coffee and not Tea and Cola}\}$ (0.20)

$$\begin{aligned} P\{\text{Coffee and Cola}\} &= P\{\text{Coffee and Tea and Cola}\} + P\{\text{Coffee and not Tea and Cola}\}, \\ \text{So } P\{\text{Coffee and not Tea and Cola}\} &= P\{\text{Coffee and Cola}\} - P\{\text{Coffee and Tea and Cola}\} \\ &= 0.25 - 0.05 = 0.20. \end{aligned}$$

(a,ii) $P\{\text{Coffee and Tea and not Cola}\}$ (0.10)

$$\begin{aligned} P\{\text{Coffee and Tea}\} &= P\{\text{Coffee and Tea and Cola}\} + P\{\text{Coffee and Tea and not Cola}\}, \\ \text{So } P\{\text{Coffee and Tea and not Cola}\} &= P\{\text{Coffee and Tea}\} - P\{\text{Coffee and Tea and Cola}\} \\ &= 0.15 - 0.05 = 0.10. \end{aligned}$$

(a,iii) $P\{\text{Tea and not Cola}\}$ (0.15)

$$\begin{aligned} P\{\text{Tea and not Cola}\} &= P\{\text{Coffee and Tea and not Cola}\} + P\{\text{not Coffee and Tea and not Cola}\}, \\ &= 0.10 + 0.05 = 0.15. \end{aligned}$$

(a,iv) $P\{\text{Tea and Cola}\}$ (0.10)

$$\begin{aligned} P\{\text{Tea}\} &= P\{\text{Tea and Cola}\} + P\{\text{Tea and not Cola}\}, \\ \text{So } P\{\text{Tea and Cola}\} &= P\{\text{Tea}\} - P\{\text{Tea and not Cola}\} = 0.25 - 0.15 = 0.10 \end{aligned}$$

(a,v) $P\{\text{not Coffee and Tea and Cola}\}$ (0.05)

$$\begin{aligned} P\{\text{Tea and Cola}\} &= P\{\text{Coffee and Tea and Cola}\} + P\{\text{not Coffee and Tea and Cola}\}, \\ \text{So } P\{\text{not Coffee and Tea and Cola}\} &= P\{\text{Tea and Cola}\} - P\{\text{Coffee and Tea and Cola}\} = \\ &= 0.10 - 0.05 = 0.05 \end{aligned}$$

(a,vi) $P\{\text{not Coffee and not Tea and Cola}\}$ (0.15)

$$\begin{aligned} P\{\text{Cola}\} &= P\{\text{not Coffee and not Tea and Cola}\} + P\{\text{Coffee and Cola}\} + P\{\text{not Coffee and Tea and Cola}\}, \\ \text{So } P\{\text{not Coffee and not Tea and Cola}\} &= P\{\text{Cola}\} - P\{\text{Coffee and Cola}\} - P\{\text{not Coffee and Tea and Cola}\} \\ &= 0.45 - 0.25 - 0.05 = 0.15 \end{aligned}$$

(b,i) $P\{\text{Coffee or Tea}\}$ (0.65)

$$= P\{\text{Coffee}\} + P\{\text{Tea}\} - P\{\text{Coffee and Tea}\} = 0.55 + 0.25 - 0.15 = 0.65.$$

(b,ii) $P\{(\text{Coffee or Tea}) \text{ or } (\text{not Coffee and not Tea and Cola})\}$ (0.80)

$$\begin{aligned} &= P\{\text{Coffee or Tea}\} + P\{\text{not Coffee and not Tea and Cola}\} - 0 \quad (\text{since mutually exclusive}), \\ &= 0.65 + 0.15 = 0.80 \end{aligned}$$

(b,iii) $P\{\text{Coffee or Tea or Cola}\}$ (0.80)

$$= P\{(\text{Coffee or Tea}) \text{ or } (\text{not Coffee and not Tea and Cola})\} = 0.80$$

(b,iv) $P\{\text{not (Coffee or Tea or Cola)}\}$ (0.20)

$$= 1 - P\{\text{Coffee or Tea or Cola}\} = 1 - 0.80 = 0.20$$